

1. Let $\begin{array}{l} z_1 = 6+2i \\ z_2 = 5-7i \end{array}$. Find $\begin{array}{l} (a) z_1 + z_2 \\ (b) z_1 - z_2 \\ (c) z_1 z_2 \\ (d) \frac{z_1}{z_2} \end{array}$

a) $6+2i + 5-7i = \underline{11-5i}$

c) $(6+2i)(5-7i) = 30 - 42i + 10i - 14i^2$

b) $6+2i - (5-7i) = 6+2i - 5+7i = \underline{1+9i}$

$= 30 - 32i + 14$

$= \underline{44-32i}$

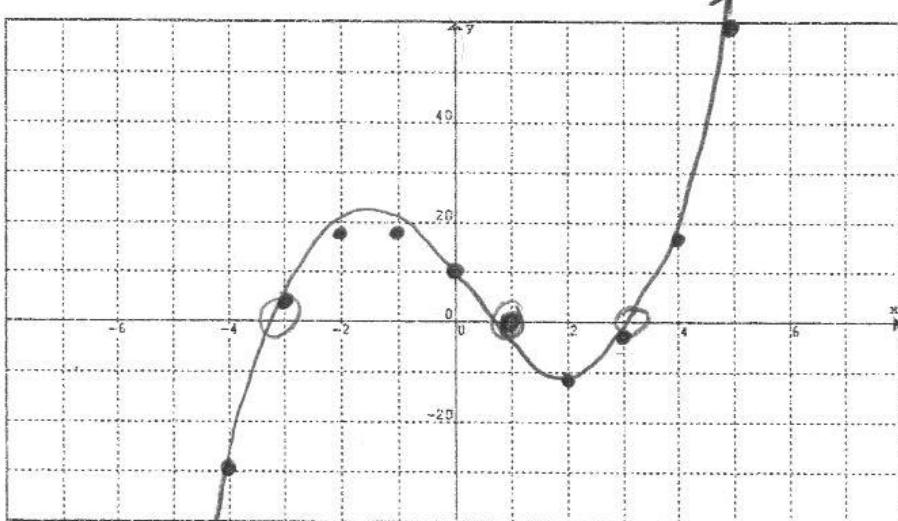
2. Consider the polynomial function $f(x) = x^3 - x^2 - 10x + 10$.

a. This function is not a quadratic function, so what is it?

Cubic

b. Use synthetic substitution to evaluate the function at the given integer x values.

c. Plot each of these points on the graph to form a continuous curve.



x	$f(x)$
-4	-30
-3	4
-2	18
-1	18
0	10
1	0
2	-6
3	-2
4	18
5	60

d. According to the graph, how many *real* zeroes will there be?

3 real zeros

e. Find all the zeroes including any imaginary solutions.

$$\begin{array}{r} 1 \mid 1 & -1 & -10 & 10 \\ & \downarrow & 0 & -10 & 0 \\ & 1 & 0 & -10 & 0 \end{array} \quad (x-1)(x^2-10)$$

Zeros: $x = 1$ or $x = \pm\sqrt{10}$

3. Use synthetic substitution or direct substitution to quickly find the remainder when the polynomial on the left is divided by the linear binomial on the right.

a. $3x^3 + 7x^2 - 12x + 1$ by $x + 3$

$$\begin{array}{r} -3 \mid 3 & 7 & -12 & 1 \\ & \downarrow & -9 & 6 & 18 \\ & 3 & -2 & -6 & 18 \end{array} \quad \text{remainder } 18$$

b. $x^{2000} + 2000$ by $x - 1$

$$(1)^{2000} + 2000 = \boxed{2001} \quad \text{remainder } 2001$$